

# Lesson 7-2

Objective - To compare and contrast congruence and similarity.

**Congruent** -  $\cong$   
- Same size and same shape.

**Similar** -  $\sim$   
- Same shape.

$\triangle ABC \cong \triangle XYZ$

$\cong$  Angles       $\cong$  Sides  
 $\angle A \cong \angle Y$        $\overline{AB} \cong \overline{XY}$   
 $\angle B \cong \angle X$        $\overline{BC} \cong \overline{XZ}$   
 $\angle C \cong \angle Z$        $\overline{AC} \cong \overline{YZ}$

$\triangle ABC \sim \triangle MLN$

$\cong$  Angles      Proportional Sides  
 $\angle A \cong \angle M$        $\frac{\overline{AB}}{\overline{ML}} = \frac{\overline{BC}}{\overline{LN}} = \frac{\overline{AC}}{\overline{MN}}$   
 $\angle B \cong \angle L$        $\frac{8}{4} = \frac{6}{3} = \frac{10}{5}$   
 $\angle C \cong \angle N$       2:1 ratio  
**Scale factor = 2**

Find the missing angles.

1)  $\triangle ABC \sim \triangle DBE$

$m\angle BDE = 60^\circ$   
 $m\angle BAC = 60^\circ$   
 $m\angle ADE = 120^\circ$

2)  $\triangle LMP \sim \triangle OMN$

$m\angle NMO = 40^\circ$   
 $m\angle P = 55^\circ$   
 $m\angle N = 55^\circ$

Find the missing sides.

1)  $\triangle HIJ \sim \triangle ABC$

$AC = 12$  un.       $IJ = 5$  un.

$\frac{3}{9} = \frac{4}{x}$        $\frac{3}{9} = \frac{y}{15}$   
 $\frac{3x}{3} = \frac{36}{3}$        $\frac{45}{9} = \frac{9y}{9}$   
 $x = 12$        $5 = y$

Find the missing sides.

2)  $\triangle QRU \sim \triangle TRS$

$QR = 10$  in.       $RU = 14$  in.

$\frac{4}{8} = \frac{5}{x}$        $\frac{4}{8} = \frac{7}{y}$   
 $\frac{4x}{4} = \frac{40}{4}$        $\frac{4y}{4} = \frac{56}{4}$   
 $x = 10$        $y = 14$

Find the missing sides.

1)  $\triangle HIL \sim \triangle HJK$

$HJ = 20$  un.       $LK = 12$  un.

$\frac{3}{12} = \frac{5}{x}$        $\frac{3}{12} = \frac{4}{y}$   
 $\frac{3x}{3} = \frac{60}{3}$        $\frac{3y}{3} = \frac{48}{3}$   
 $x = 20$        $y = 16$

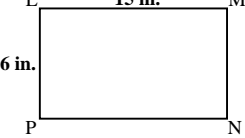
If a new rectangle has three times the length and width of the original rectangle, how would the perimeters and areas compare?

	Original	New
Dimension	3  4	9  12
1-D {	Width w = 3	w = 9
	Length l = 4	l = 12
Perimeter	P = 2(3)+2(4) P = 6+8 = 14 un.	P = 2(9)+2(12) P = 18+24 = 42 un.
2-D {	Area A = 1 • w A = 4 • 3 = 12 un <sup>2</sup>	A = 1 • w A = 12 • 9 = 108 un <sup>2</sup>

*Note: The perimeter comparison shows a 3x increase, and the area comparison shows a 9x increase.*

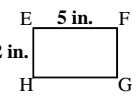
## Lesson 7-2

Rectangle EFGH ~ Rectangle LMNP



15 in.

6 in.



5 in.

2 in.

Sides are 3 times as long. **Scale factor = 3.**

Perimeter	Area
$P_{LMNP} = 42 \text{ in.}$ $P_{EFGH} = 14 \text{ in.}$	$A_{LMNP} = 90 \text{ in}^2$ $A_{EFGH} = 10 \text{ in}^2$
$\left. \begin{array}{l} P_{LMNP} = 42 \text{ in.} \\ P_{EFGH} = 14 \text{ in.} \end{array} \right\} \text{ratio } 3:1$	$\left. \begin{array}{l} A_{LMNP} = 90 \text{ in}^2 \\ A_{EFGH} = 10 \text{ in}^2 \end{array} \right\} \text{ratio } 9:1$
<b>Ratio of Perimeters = Scale Factor</b>	<b>Ratio of Areas = Square of Scale Factor</b>

Scale Drawings

The scale on a blueprint reads 1 in:12ft. If the length of the building in the blueprint is 13 inches, what is the actual length of the building?

Let  $x$  = actual length of building

$\frac{\text{map}}{\text{actual}}$	$\frac{1 \text{ in.}}{12 \text{ ft.}} = \frac{13 \text{ in.}}{x}$
	$1x = 12(13)$
	$x = 156 \text{ feet}$